

Theoretical and Experimental Investigation of Thermodynamics and Kinetics of Thiol-Michael Addition Reactions: A Case Study of Reversible Fluorescent Probes for Glutathione Imaging in Single Cells

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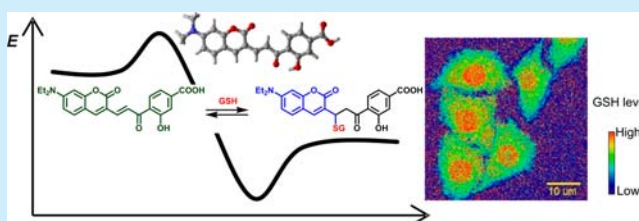
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S Supporting Information

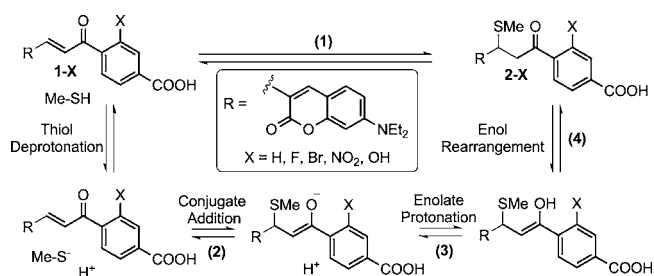
ABSTRACT: Density functional theory (DFT) was applied to study the thermodynamics and kinetics of reversible thiol-Michael addition reactions. M06-2X/6-31G(d) with the SMD solvation model can reliably predict the Gibbs free energy changes (ΔG) of thiol-Michael addition reactions with an error of less than 1 kcal·mol⁻¹ compared with the experimental benchmarks. Taking advantage of this computational model, the first reversible reaction-based fluorescent probe was developed that can monitor the changes in glutathione levels in single living cells.



Michael addition reactions have recently gained increasing interest in many different fields, including bioconjugation chemistry, design of irreversible small molecule inhibitors, and development of molecular imaging probes.^{1–3} An example of a Michael addition commonly used for bioconjugation is the thiol-maleimide reaction. This reaction is considered one of the “click” reactions due to its fast reaction rate and aqueous compatibility.¹ Some investigational and approved drugs, including afatinib and neratinib, also contain a Michael acceptor moiety, which can irreversibly react with the cysteine residue in the active site to achieve inhibition of the targeted proteins.² In addition, taking advantage of the reversibility of thiol Michael addition reactions, our group recently reported the first fluorescent probe for quantitative glutathione (GSH) imaging in living cells.³

Due to the broad applications of thiol-Michael addition reactions, it is highly desirable to improve our understanding of the reaction mechanisms and predict the reactivities between thiols and Michael acceptors using computational chemistry.^{4–6} A generally accepted reaction mechanism for thiol-Michael addition begins with deprotonation of the thiol, followed by conjugate addition of the thiolate to the β -position of the Michael acceptor to form an enolate (Scheme 1). Houk and co-workers tested a series of density functional theory (DFT) based methods to calculate the activation energies and Gibbs free energies of the conjugate additions of MeSH to six α,β -unsaturated ketones and concluded that M06-2X, along with two other DFT methods, gives results within 1 kcal·mol⁻¹ of the CBS-QB3 benchmark values.⁶ It should be noted that despite the fact that the B3LYP DFT functional has been widely used in computational

Scheme 1. General Scheme for the Mechanism of Thiol-Michael Addition Reactions^a



^aCompounds 1-X are the GSH probes investigated in this study.

chemistry, it predicted the energies of thiol Michael additions with substantial inaccuracies.⁶ Rowley and co-workers suggested that range-separated DFT functionals can improve the accuracy in calculating the energies of thiol Michael additions.⁵ In both Houk and Rowley's studies, the accuracies of the DFT methods were compared to high level *ab initio* calculations as benchmarks instead of experimental values. Rosenker et al. studied the energetics of thiol addition and elimination reactions to bicyclic enones in organic solvents using ¹H NMR and DFT calculations and found excellent agreement between experiments and theory.⁴ Flanagan et al. measured the addition reaction kinetics

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between a series of acrylamides and GSH in phosphate buffers (pH 7.4) and found that the calculated activation energies are well correlated with the measured reaction rates ($R^2 = 0.915$).⁷ However, due to the low propensity of thiol elimination from the adducts for the bicyclic enones and the acrylamides, the reverse reactions were not investigated and the equilibrium constants of these reactions cannot be accurately measured.

In our previous development of GSH probe ThiolQuant Green (TQG), we identified TQG, which had an appropriate equilibrium constant K_d when reacting with GSH. Unfortunately, both the forward and reverse reaction rates between TQG and GSH are slow; thus, the probe only allows one-point measurements and is unsuitable for following the changes in GSH levels in single cells.³ Our goal in this study is 2-fold: to evaluate the accuracies of DFT calculations in predicting the equilibrium constants and reaction kinetics for thiol-Michael addition reactions in aqueous environment using experimental values as benchmarks; and to accelerate the reaction rate of our GSH probe through systematic structural variation and apply the newly developed probe to monitor GSH level changes in single cells for the first time.

A series of TQG analogues were synthesized (1-X, Scheme 1). All the GSH probes showed absorption maxima around 488 nm (representative spectra of 1-OH are shown in Figure 1). Upon

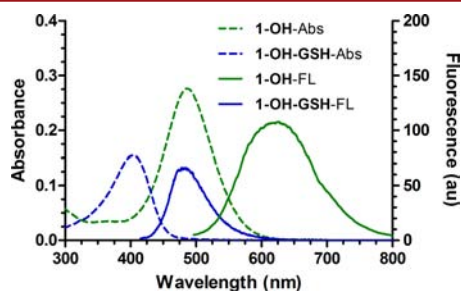


Figure 1. UV-vis and fluorescence spectra of GSH probe 1-OH ($\lambda_{ex} = 485$ nm) and 1-OH-GSH ($\lambda_{ex} = 405$ nm) in PBS. The spectra of 1-OH-GSH were obtained by measuring the mixture of 1-OH (15 μ M) and GSH (80 mM) in PBS.

reacting with GSH in a phosphate-buffered saline at pH 7.4 (PBS), the absorption and fluorescence peaks of these GSH probes shift hypsochromically (Figure 1). The equilibrium constants between the probes 1-X and GSH were measured by incubating the probes with a series of concentrations of GSH (0.1–80 mM) in PBS under anaerobic conditions for 24 h to ensure equilibrium had been established. It should be noted that due to the reversible nature of the reactions, the ratiometric spectrometric changes of these probes are GSH concentration-dependent instead of time-dependent as we demonstrated previously.³ The K_d values for the reaction between the probes 1-X and GSH were calculated based on the corresponding absorption changes in different concentrations of GSH solutions (Supporting Information (SI), Figure S1). As shown in Table 1, the K_d values are in the range of 0.25–1.43 mM (please refer to the SI for the detailed procedure to calculate the K_d values).

In order to calculate the K_d values, we employed the M06-2X DFT method following Houk's previous work.^{4,6} To simplify the calculations, methylthiol was used to substitute GSH. The Gibbs free energies of thiol-Michael addition reactions (reaction 1 in Scheme 1) were initially calculated by optimizing the geometries of reactants and products in the gas phase with frequency analyses at the M06-2X/6-31G(d) level of theory. Unfortunately,

Table 1. Experimental and Calculated Thermodynamic and Kinetic Parameters for GSH Probes 1-X^a

X	experiments				calculations		
	K_d^b	k_f^c	k_r^d	ΔG^e	ΔG_1^e	ΔG_2^e	ΔG_3^e
H	0.42	0.052	4.7	-4.7	-4.9	-2.6	-35.5
F	0.51	0.10	11.5	-4.6	-4.4	-3.1	-34.4
Br	1.35	0.15	35.7	-4.0	-4.8	-3.2	-34.4
NO ₂	1.43	0.18	46.6	-3.9	-4.0	-5.0	-34.1
OH	0.25	1.29	6050	-5.0	-4.7	-6.0	-30.0

^a K_d , k_f , and k_r are the dissociation equilibrium constant, the second-order forward reaction rate constant, and the first-order reverse reaction rate constant of reaction 1 in Scheme 1, respectively. ^bUnits are in mM. ^cUnits are in $M^{-1} s^{-1}$. ^dUnits are in $10^{-6} s^{-1}$. ^eUnits are in $kcal \cdot mol^{-1}$. Refer to Scheme S3 in the SI for definitions of ΔG_1 , ΔG_2 , and ΔG_3 .

we found that the calculated ΔG in the gas phase (-8.38 $kcal \cdot mol^{-1}$) deviated significantly from the experimental values in water (-3.97 $kcal \cdot mol^{-1}$) and concluded that the solvation energies are important to accurately predict the energies of Michael addition reactions. We reoptimized all the reactant and product structures in water using the same DFT functional with the SMD solvation model. As shown in Table 1, accounting for the solvation energies resulted in the calculated Gibbs free energies ΔG_1 in excellent agreement with the experimental values ΔG . In Houk's study, most of the experimental ΔG values for thiol-enone Michael addition reactions were estimated to be ≤ -4.6 $kcal \cdot mol^{-1}$ due to the sensitivity limit of NMR measurements, which renders it impossible to evaluate the accuracy of the calculated ΔG values.⁴ In our study, all the model reactions were carefully chosen in order to provide precisely measurable ΔG values. It should be noted that the calculated ΔG for 1-Br related reactions has the largest error (0.8 $kcal \cdot mol^{-1}$), which could be due to the relatively small basis set used. We attempted to recalculate the bottom-of-well electronic energies using a large basis set 6-311G(2d,p) and other DFT methods at the M06-2X/6-31G(d) geometries and found that the calculated ΔG values have large deviations from the experimental benchmarks (refer to SI for details). Therefore, we concluded that M06-2X/6-31G(d) with the SMD solvation model can reliably predict the Gibbs free energy changes of Michael addition reactions, at least in water, with an error of less than 1 $kcal \cdot mol^{-1}$ (Table 1).

We also measured the kinetic parameters of both forward and reverse thiol-Michael addition reactions. The forward reaction rate constants k_f were determined by monitoring the time-dependent absorption changes of the GSH probes 1-X (479 nm) and the GSH adducts 1-X-GSH (405 nm) when reacting with GSH in PBS (SI, Figure S2). The pseudo first-order rate constants k_f' were calculated based on a monoexponential global fitting of the decay and growth of the absorbance at 479 and 405 nm, respectively. The second order rate constants k_f were calculated based on k_f' (Table 1). The reverse reaction rate constants k_r were measured using pre-equilibrated mixtures of 1-X and GSH with addition of 5,6-dihydro-2H-pyran-2-one as a GSH scavenger to initiate the retro-Michael addition process (SI, Figure S2). The first order rate constants k_r were calculated based on a monoexponential global fitting of the decay and growth of the absorbance at 405 and 479 nm, respectively (Table 1). It is interesting to note that a faster forward reaction rate is always associated with a faster reverse reaction rate (Table 1).

Precisely predicting the solution-phase reaction rates using computational chemistry is nontrivial due to the difficulty of predicting absolute free energies of solvation for ions and inaccurate estimation of the pre-exponential factors in the Arrhenius equation.⁸ In other studies, the M06-2X functional has been applied to compare the energy barriers of different reaction pathways and to predict the kinetic isotope effects.⁹ We attempted to locate the transition state structures of the Michael addition reactions using M06-2X/6-31G(d) with the SMD solvation model, but to no avail. This may be because the attack of the thiolate on the enones has a very small enthalpy barrier, resulting in difficulty in identifying the transition state on the potential energy surface. Based on the Hammett's linear free-energy relationship, a more exothermic reaction in the rate-determining step (RDS) has a lower activation energy barrier. Previous studies established that thiolate conjugate addition (reaction 2 in Scheme 1) is the RDS in Michael addition reactions.⁶ Therefore, in order to qualitatively compare the reaction rates between the GSH probes, we calculated the Gibbs free energy changes (ΔG_2 in Table 1) for the thiolate conjugate addition reactions. Plotting ΔG_2 versus $\log k_f$ afforded a fair linear relationship (SI, Figure S3, $R^2 = 0.84$). Among the GSH probes investigated, compound **1-OH** shows the fastest forward reaction rate. This may be due to the hydrogen bonding between the hydroxyl and the carbonyl groups, which stabilizes the enolate intermediate (SI, Figure S4).¹⁰ Regarding the reverse reactions, the enolate intermediate should be formed based on the principle of microscopic reversibility. Thurlar and co-workers provided computational analysis for the reaction mechanisms of α,β -elimination of esters and thioesters to support a stepwise first-order elimination from a conjugate base (E1cB) mechanism.¹¹ Based on our computational data, we found that plotting $-\Delta G_3$ versus $\log k_r$, but not $-\Delta G_1$, $-\Delta G_2$, nor $-\Delta G_4$, afforded an excellent linear relationship (SI, Figure S5, $R^2 = 0.97$), which demonstrates that the formation of the enolate intermediates is the RDS for retro-Michael addition reactions and supports an E1cB mechanism.

With the extensive theoretical and experimental investigation of Michael addition reactions, we identified **1-OH** as an improved GSH probe that has faster kinetics than **TQG**. As in our previous study, we applied acetoxyethyl (AM) ester to facilitate cell uptake of the probe, which is designated as **1-OH-AM** (Figure 2). The procedure to apply **1-OH-AM** for GSH

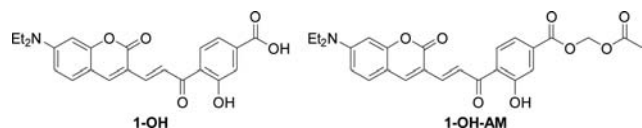


Figure 2. Chemical structures of GSH probe (**1-OH**) and its cell-permeable form (**1-OH-AM**).

measurements in cells is similar to that for **TQG**. As shown in Figure 3, HeLa cells were incubated with **1-OH-AM** ($1 \mu\text{M}$) for 30 min and imaged using a confocal microscope with both 405 and 488 nm excitations. The ratiometric images (Figure 3D) were generated by dividing the fluorescence intensity values for the 405 nm channel (Figure 3A) by the 488 nm channel (Figure 3B) at each corresponding pixel. The ratio values are proportional to the GSH concentrations.

Taking advantage of the reaction reversibility and fast reaction kinetics of **1-OH**, we were able to observe the GSH level changes in single cells for the first time. To illustrate the ability of **1-OH** to

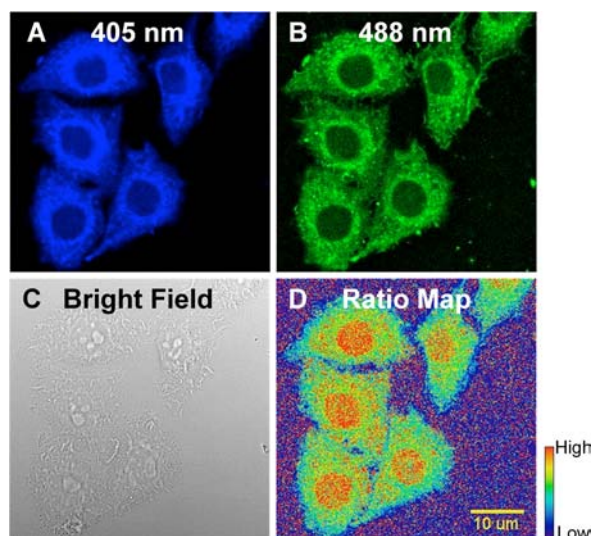


Figure 3. Confocal images and ratio map of HeLa cells stained with **1-OH-AM**. Fluorescent images were acquired with (A) $\lambda_{\text{ex}} = 405 \text{ nm}$, $\lambda_{\text{em}} = 418\text{--}495 \text{ nm}$; and (B) $\lambda_{\text{ex}} = 488 \text{ nm}$, $\lambda_{\text{em}} = 499\text{--}695 \text{ nm}$. (C) Bright field image. (D) The ratio map was calculated by dividing the fluorescence intensity values for the 405 nm channel by the 488 nm channel at each corresponding pixel. The ratio values are proportional to the GSH concentrations. In the rainbow scale bar, red and blue represent high and low GSH concentrations, respectively.

monitor GSH dynamics, a GSH-ester solution ($100 \mu\text{M}$) was added to the imaging plate to transiently increase the intracellular level of GSH, and the same cells were imaged again. Based on the ratiometric images in Figure 4A, we observed an increase in the GSH level in all cells imaged as expected. In a similar experiment, an *N*-ethylmaleimide (NEM) solution ($100 \mu\text{M}$) was used as a GSH scavenger and a decrease in the ratio was observed in accordance with the GSH concentration decrease (Figure 4B). Therefore, **1-OH-AM** can be a powerful tool to monitor the GSH level changes in single cells upon biological stimulation.

It should be noted that GSH probes based on irreversible reactions or reversible reactions with inappropriate K_d in aqueous environment^{12–14} can only reflect the difference in GSH levels in bulk cell lysates or in different cells, but cannot follow the GSH level changes in an individual cell. Furthermore, due to the sluggish reverse reaction rate of **TQG**, it only allows one-point measurements and is unsuitable for following the changes in GSH levels in single cells.³ Kim et al. reported a GSH probe with a similar structure but without the aqueous solubilizing carboxylic acid group.¹⁰ We synthesized Kim's GSH probe and found it has little aqueous solubility. Kim et al. measured the second-order rate constant between his probe and β -mercaptoethanol to be $6.98 \times 10^{-2} \text{ M}^{-1} \text{ s}^{-1}$, which is only $\sim 5\%$ of the reaction rate for **1-OH**. Therefore, due to the hydrophobicity of Kim's GSH probe, it reacts very slowly with GSH both in the forward and reverse reactions and cannot be used to monitor the GSH level changes in single cells.

In summary, we evaluated a small library of **TQG** analogues and identified **1-OH** as an improved GSH probe that allows for the monitoring of changes in GSH levels in single cells. We extensively measured the thermodynamic and kinetic parameters for the reactions between GSH and the probes, which can serve as experimental benchmarks to evaluate the accuracy of computational methods. We found that M06-2X/6-31G(d) with the SMD solvation model can precisely predict the Gibbs free energy changes for the Michael addition reactions with an

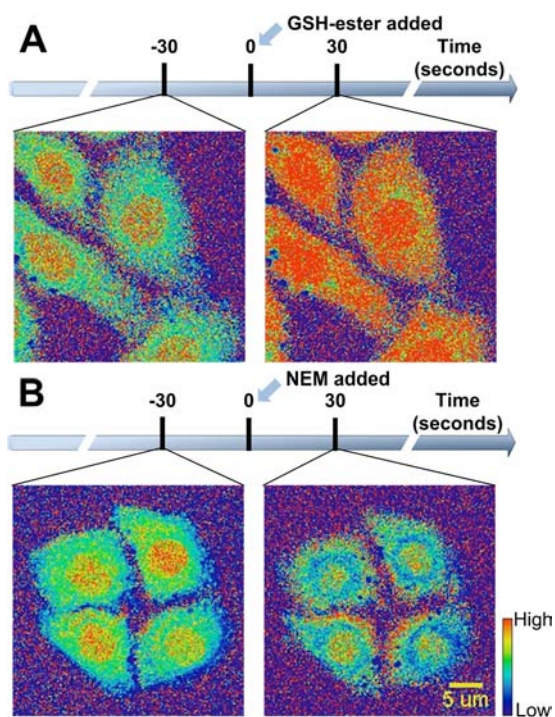


Figure 4. Time-lapsed ratiometric imaging of the changes of GSH levels in single cells. While HeLa cells were imaged under a confocal microscope, (A) GSH-ester (100 μM) and (B) NEM (100 μM) were added to the culture medium to induce increase and decrease of GSH levels, respectively. The ratiometric images shown are 30 s before and after inducing the changes of GSH levels. In the rainbow scale bar, red and blue represent high and low GSH concentrations, respectively.

error within 1 kcal·mol⁻¹ when compared with the experimental benchmarks. We also discovered that the reaction kinetics of the Michael addition reactions can be qualitatively predicted based on the Gibbs free energy changes of the thiolate conjugate addition reactions. Although this strategy cannot accurately predict the reaction rates, it serves as a convenient method for qualitatively comparing the reaction kinetics of Michael addition reactions without locating the transition states. In addition, our calculations support an E1cB mechanism for the retro-Michael addition reaction, in which the formation of the enolate anions is the RDS. Therefore, this study not only provided a convenient computational method to predict the thermodynamics and kinetics of Michael addition reactions but also developed the first probe that can monitor GSH level changes in single cells, which is expected to be a powerful tool in redox biology studies.

■ ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.orglett.5b02910.

Experimental details for organic synthesis, computational studies, and cell imaging studies (PDF)

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Notes

The authors declare no competing financial interest.

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■ REFERENCES

- (1) Saito, F.; Noda, H.; Bode, J. W. *ACS Chem. Biol.* **2015**, *10*, 1026.
- (2) Zhang, X.; Munster, P. N. *Expert Opin. Pharmacother.* **2014**, *15*, 1277.
- (3) Jiang, X.; Yu, Y.; Chen, J.; Zhao, M.; Chen, H.; Song, X.; Matzuk, A. J.; Carroll, S. L.; Tan, X.; Sizovs, A.; Cheng, N.; Wang, M. C.; Wang, J. *ACS Chem. Biol.* **2015**, *10*, 864.
- (4) Rosenker, C. J.; Krenske, E. H.; Houk, K. N.; Wipf, P. *Org. Lett.* **2013**, *15*, 1076.
- (5) Smith, J. M.; Jami Alahmadi, Y.; Rowley, C. N. *J. Chem. Theory Comput.* **2013**, *9*, 4860.
- (6) Krenske, E. H.; Petter, R. C.; Zhu, Z.; Houk, K. N. *J. Org. Chem.* **2011**, *76*, 5074.
- (7) Flanagan, M. E.; Abramite, J. A.; Anderson, D. P.; Aulabaugh, A.; Dahal, U. P.; Gilbert, A. M.; Li, C.; Montgomery, J.; Oppenheimer, S. R.; Ryder, T.; Schuff, B. P.; Uccello, D. P.; Walker, G. S.; Wu, Y.; Brown, M. F.; Chen, J. M.; Hayward, M. M.; Noe, M. C.; Obach, R. S.; Philippe, L.; Shanmugasundaram, V.; Shapiro, M. J.; Starr, J.; Stroh, J.; Che, Y. *J. Med. Chem.* **2014**, *57*, 10072.
- (8) Marenich, A. V.; Olson, R. M.; Kelly, C. P.; Cramer, C. J.; Truhlar, D. G. *J. Chem. Theory Comput.* **2007**, *3*, 2011.
- (9) Zhao, Y.; Truhlar, D. G. *Chem. Phys. Lett.* **2011**, *502*, 1.
- (10) Kim, G. J.; Lee, K.; Kwon, H.; Kim, H. J. *Org. Lett.* **2011**, *13*, 2799.
- (11) Kim, Y.; Mohrig, J. R.; Truhlar, D. G. *J. Am. Chem. Soc.* **2010**, *132*, 11071.
- (12) Chan, J.; Dodani, S. C.; Chang, C. J. *Nat. Chem.* **2012**, *4*, 973 and references therein..
- (13) Yin, C.; Huo, F.; Zhang, J.; Martinez-Manez, R.; Yang, Y.; Lv, H.; Li, S. *Chem. Soc. Rev.* **2013**, *42*, 6032 and references therein..
- (14) Jung, H. S.; Chen, X.; Kim, J. S.; Yoon, J. *Chem. Soc. Rev.* **2013**, *42*, 6019 and references therein..